SIE 550 (Linear) Systems Theory: Spring 2025

Course Instructor, Lectures and Course Website

Instructor: Dr. Roberto Furfaro, robertof@arizona.edu

1. Campus Office: ENGR305, 520-621-2525

2. Cell: 520-312-7440 (texting is preferred)

<u>Office Hours:</u> Tue-Th 3pm-4pm or by appointment. <u>Teaching Assistant:</u> TBD (OH: for TAs will be announced later) <u>Lectures:</u> Tue-Th, 4:00pm - 5:15pm (In-person/Zoom) <u>Course content on D2L:</u> <u>www.d2l.arizona.edu</u>

Course Description

This course is a core course for graduate students at the SIE department. Although the title is "Linear Systems Theory", the course will cover both linear and non-linear systems under a unified framework. The goal of the course is to give the students a deep understanding of the behavior of dynamical systems as well as means to analyze autonomous and non-autonomous systems employing basic and advanced mathematical techniques. The material covered in this course spans from representation and analysis of dynamical systems, Lyapunov stability theory, controllability and observability of linear systems as well as design techniques for dynamical system stabilization.

Schedule and Topics

Week 0: Jan 16

Topic: Introduction

Week 1: Jan 21 -23

Topic: Mathematical Background: Fundamentals of linear algebra

- 1. Vector spaces
- 2. Linear Operators
- 3. Eigenvalues and Eigenvectors
- 4. Diagonal Forms and Jordan Forms
- 5. Special Linear Operators: Symmetric and Normal/Orthogonal Operators

Week 2: Jan 28-30

Topic: Linear and Non-Linear Dynamical Systems

- 1. General Dynamical Models
- 2. Examples of linear and non-linear models
- 3. Linear and non-linear phenomena

Week 3: Feb 4– Feb 6

Topic: Solutions of Linear Differential Equations

- 1. Solution of Systems of linear differential Equations
- 2. Laplace transform and the concept of transfer function
- 3. Duality

Wed Feb 5 - HW#1 due

Week 4: Feb 11 – 13

Topic: Stability Concepts I

- 1. Stability of Equilibrium Points and Linearization
- 2. Lyapunov Stability: General Concepts
- 3. Lyapunov Stability for Linear Systems

Week 5: Feb 18-20

Topic: Stability Concepts II

- 1. Lyapunov Stability for Non-linear Systems and Linearization
- 2. Exponential Stability and Region of Attraction
- 3. Converse Lyapunov Functions and Non-Autonomous Systems

Wed Feb 19 – HW#2 Due

Week 6: Mar 4 – Mar 6

Topic: Stability Concepts III

- 1. Perturbed Systems
- 2. BIBO Stability

Week SB (Mar 8- Mar 15): Spring Recess

Week RW (Review): Mar 18-20

<u>Topic: Review and Mid-Term Exam</u> **Tue Mar 18** - Midterm Review **Th Mar 20** - Midterm Exam

Wed Mar 19 – HW#3 Due

Week 7: Mar 25 – Mar 27

Topic: Finite Time Stability

- 1. Finite Time Stability: Basic Concept and Definitions
- 2. Finite Time Stability Conditions for Autonomous and Non-Autonomous Systems

Week 8: Apr 1 – Apr 3

Topic: Controllability

- 1. General Conditions
- 2. Controllability Canonical Forms
- 3. Time Invariant Systems

- 4. Output and Trajectory Controllability
- 5. Controllability and Stability for General Systems

Week 9: Apr 8 – Apr 11

Topic: Observability

- 1. General Conditions
- 2. Observability Canonical Forms
- 3. Time Invariant Systems

Wed Apr 10 - HW# 4 due

Week 10: Apr 15 – Apr 17

Topic: Canonical Forms

- 1. Controllability Canonical Forms
- 2. Observability Canonical Forms
- 3. Examples

Week 11: Apr 22 – Apr 24

Topic: Systems Design and Estimation I: Linear Methods

- 1. Stabilization: Basic Concepts and Linearization
- 2. Linear Systems Design: Eigenvalues placements
- 3. Linear Systems Observers
- 4. Controller Observer Separation Theorem
- 5. Examples

Wed Apr 23 – HW#5 due

Week 12: Apr 29 – May 1

Topic: Systems Design and Estimation II: Linear Methods

- 1. Design and Estimation examples via MATLAB
- 2. Linear Quadratic Regulator

Week 13: May 6

<u>Topic: Final Review</u> **Tue May 6** - Final Review **Wed May 7** – HW#6 due

Final Exam: 4-6pm, May 12, 2025

Grading

A regular grade (A, B, C, D, E) will assigned. The grade will be established as function of the class performance (curve). Each student will receive a numerical value according to his/her performance on the following items:

Midterm Exam	30%
Final Exam	40%

Homework

30%

Course Objectives

At the end of the course, the students are expected to be able to:

- 1. Analyzing of Linear and Non-Linear Dynamical Systems
- 2. Applying of the Lyapunov Stability Theory to Dynamical Systems
- 3. Understanding if a System is Controllable and Observable
- 4. Applying a Variety of Design Methodologies to Stabilize Dynamical Systems

Semester Assignments, Midterm and Final Examination

During the semester, students will be required to submit approximately 6 (six) homeworks with bi-weekly frequency. Homeworks will be a combination of theoretical analysis and limited computer simulation via MATLAB. There will be one mid-term exam and one comprehensive final exam. Considering the pandemic instructions on both exams format will be announced later. Make-up exams for a valid excuse must be arranged at least <u>1 week before</u> the scheduled exam date. Emergency situation should be communicated to the instructor as soon as possible to arrange for an alternative schedule. Without prior consent, there will be no make-up exams.

Class Attendance, Participation and General Ethical Guidelines

The students are expected to regularly attend the lectures. If lectures are missed, the student should make sure you get up-to-date with the course material by reviewing the zoom recorded lectures and the material posted on the D2L course website. Students and faculty each have a responsibility for maintaining an appropriate learning environment. Those who fail to adhere to such behavioral standards may be subject to discipline. Active participation during classes (e.g. answering questions when asked by the instructor, show interest and motivation for the subject) is encouraged and it may be taken into account when establishing the final grade. While collaboration and discussion between students during homework is encouraged, plagiarism is not tolerated and may be subjected to disciplinary actions.

Textbooks

Szidarovszky and Bahill, Linear Systems Theory, Second Edition (Systems Engineering) Hardcover – November 25, 1997 (Required).

Instructor class notes and relevant material (the instructor will make them available through the D2L course website at d2l.arizona.edu)

Software

MATLAB (full version available for download to UA students)

Zoom Lectures

Lectures will be delivered via zoom – access is granted via D2L portal. Here you have the zoom invitation:

NOTE: Password: 123321

Roberto Furfaro is inviting you to a scheduled Zoom meeting.

This meeting was created in a non-BAA environment and is not intended for the discussion of healthcare, health education, or health data research.

Topic: SIE 550 SP25 001 025 110 210 Time: Jan 16, 2025 04:00 PM Arizona Every week on Tue, Thu, until May 6, 2025, 32 occurrence(s) Jan 16, 2025 04:00 PM Jan 21, 2025 04:00 PM Jan 23, 2025 04:00 PM Jan 28, 2025 04:00 PM Jan 30, 2025 04:00 PM Feb 4, 2025 04:00 PM Feb 6, 2025 04:00 PM Feb 11, 2025 04:00 PM Feb 13, 2025 04:00 PM Feb 18, 2025 04:00 PM Feb 20, 2025 04:00 PM Feb 25, 2025 04:00 PM Feb 27, 2025 04:00 PM Mar 4, 2025 04:00 PM Mar 6, 2025 04:00 PM Mar 11, 2025 04:00 PM Mar 13, 2025 04:00 PM Mar 18, 2025 04:00 PM Mar 20, 2025 04:00 PM Mar 25, 2025 04:00 PM Mar 27, 2025 04:00 PM Apr 1, 2025 04:00 PM Apr 3, 2025 04:00 PM Apr 8, 2025 04:00 PM Apr 10, 2025 04:00 PM

Apr 15, 2025 04:00 PM Apr 17, 2025 04:00 PM Apr 22, 2025 04:00 PM Apr 24, 2025 04:00 PM Apr 29, 2025 04:00 PM May 1, 2025 04:00 PM May 6, 2025 04:00 PM

Please download and import the following iCalendar (.ics) files to your calendar system. Weekly: https://arizona.zoom.us/meeting/tZMlfuigqj0rG9x5UM-IOWS2NH7eULT4YPu0/ics?icsToken=DFyxdHJSG7sMC5rc5AAALAAAAKwX2uuZ0rAoFHRhzov8RS H2x5AQ8xFk HQ8BgLCQd0XF5AbVaDVy8kcSQq-ZK1CoBNFSZdjHFrQ5OiXKTAwMDAwMQ

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